		MATHS - YEAR 11		RAG
	Whole year:	Higher Tier		
1.	Integer	A whole number that can be positive, negative or zero.	-3, 0, 92	
2.	Factor	A number that divides exactly into another number without a remainder.	The factors of 18 are: 1, 2, 3, 6, 9, 18 The factor pairs of 18 are: 1, 18	
		It is useful to write factors in pairs.	2, 9 3, 6	
3.	Multiple	The result of multiplying a number by an integer.	The first five multiples of 7 are: 7, 14, 21, 28, 35	
4.	Highest Common Factor (HCF)	The times tables of a number. The biggest number that divides exactly into two or more numbers.	The HCF of 6 and 9 is 3 because it is the biggest number that divides into 6 and 9 exactly.	
5.	Lowest Common Multiple (LCM)	The smallest number that is in the times tables of each of the numbers given.	The LCM of 3, 4 and 5 is 60 because it is the smallest number in the 3, 4 and 5 times tables.	
6.	Prime Number	A number that has exactly two factors: one and itself.	The first ten prime numbers are: 2, 3, 5, 7, 11, 13, 17, 19, 23 and 29	
7.	Prime Factor	A factor which is a prime number.	The prime factors of 18 are: 2,3	
8.	Product of Prime Factors	Finding out which prime numbers multiply together to make the original number. se a prime factor tree. Also known as 'prime factorisation'.	$36 = 2 \times 2 \times 3 \times 3$ $36 = 2 \times 2 \times 3 \times 3$ or $2^2 \times 3^2$ 3 3 3	
9.	Recurring	A decimal number that has digits that repeat forever. The part that repeats is usually shown by placing a dot above the digit that repeats, or dots over the first and last digit of the repeating pattern.	$\frac{1}{3} = 0.333 \dots = 0.\dot{3}$ $\frac{1}{7} = 0.142857142857 \dots$ $= 0.\dot{1}4285\dot{7}$ $\frac{77}{600} = 0.128333 \dots = 0.128\dot{3}$	



	MATHS - YEAR 11 Higher Tier			RAG
	Whole year:			
10.	Rational number	A number of the form $\frac{p}{q}$, where p and q are integers and $q \neq 0$.	$\frac{4}{9}$, 6, $-\frac{1}{3}$, $\sqrt{25}$ are examples of rational numbers.	
11.	Irrational number	A number that cannot be written in the form $\frac{p}{q}$, where p and q are integers and $q \neq 0$.	$\pi,\sqrt{2}$ are examples of an irrational numbers.	
12.	Surd	The irrational number that is a root of a positive integer , whose value cannot be determined exactly.	$\sqrt{2}$ is a surd because it is a root which cannot be determined exactly.	
		Surds have infinite non- recurring decimals.	$\sqrt{2} = 1.41421356$ which never repeats.	
13.	Ratio	Ratio compares the size of one part to another part. Written using the ':' symbol.	3:1	
14.	Proportion	Proportion compares the size of one part to the size of the whole . Usually written as a fraction.	In a class with 13 boys and 9 girls, the proportion of boys is $\frac{13}{22}$ and the proportion of girls is $\frac{9}{22}$	
15.	Simplifying Ratios	Divide all parts of the ratio by a common factor .	5 : 10 = 1 : 2 (divide both by 5) 14 : 21 = 2 : 3 (divide both by 7)	
16.	Ratios in the form $1 : n$ or $n : 1$	Divide both parts of the ratio by one of the numbers to make one part equal 1 .	5: 7 = 1: $\frac{7}{5}$ in the form 1 : n 5: 7 = $\frac{5}{7}$: 1 in the form n : 1	
17.	Sharing in a Ratio	1. Add the total parts of the ratio.	Share £60 in the ratio 3 : 2 : 1.	
		2. Divide the amount to be shared by this value to find the value of one part.	3 + 2 + 1 = 6 60 ÷ 6 = 10	
		3. Multiply this value by each part of the ratio.	3 x 10 = 30, 2 x 10 = 20, 1 x 10 = 10	
		Use only if you know the total.	£30 : £20 : £10	



		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
18.	Proportional Reasoning	Comparing two things using multiplicative reasoning and applying this to a new situation.	7 bunches of flowers contain 42 flowers.How many flowers are in 1 bunch?+7+77 bunches42 flowers1 bunch1 bunch6 flowers	
		Identify one multiplicative link and use this to find missing quantities.		
19.	Unitary Method	Finding the value of a single unit and then finding the necessary value by multiplying the single unit value.	3 cakes require 450g of sugar to make. Find how much sugar is needed to make 5 cakes. 3 cakes = 450g So 1 cake = 150g (÷ by 3) So 5 cakes = 750 g (x by 5)	
20.	Ratio already shared	Find what one part of the ratio is worth using the unitary method .	Money was shared in the ratio 3:2:5 between Ann, Bob and Cat. Given that Bob had £16, found out the total amount of money shared.	
			£16 = 2 parts	
			So £8 = 1 part	
			3 + 2 + 5 = 10 parts, so 8 x 10 = £80	
21.	Best Buys	Find the unit cost by dividing the price by the quantity .	8 cakes for £1.28 → 16p each (÷by 8)	
		The lowest number is the best value.	13 cakes for £2.05 → 15.8p each (÷by 13)	
			Pack of 13 cakes is best value.	
22.	Percentage Change	DifferenceOriginal	A games console is bought for £200 and sold for £250. % change = $\frac{50}{200} \times 100 = 25\%$	



MATHS - YEAR 11 Higher Tier				RAG
	Whole year:			
23.	Fractions to	Divide the numerator by the	3	
	Decimals	denominator using the bus	$\frac{3}{8} = 3 \div 8 = 0.375$	
		stop method.		
24.	Decimals to	Write as a fraction over 10,	$0.36 = \frac{36}{100} = \frac{9}{25}$	
	Fractions	100 or 1000 and simplify.		
25.	Percentages to Decimals	Divide by 100.	$8\% = 8 \div 100 = 0.08$	
26.	Decimals to Percentages	Multiply by 100.	$0.4 = 0.4 \times 100\% = 40\%$	
27.	Fractions to	Percentage is just a fraction	3 12	
	Percentages	out of 100. Make the	$\frac{3}{25} = \frac{12}{100} = 12\%$	
	-	denominator 100 using		
		equivalent fractions.	$\frac{9}{17} \times 100 = 52.9\%$	
		When the denominator		
		doesn't go in to 100, use a		
		calculator and multiply the		
2.2	<u> </u>	fraction by 100.	14 7	
28.	Percentages to Fractions	Percentage is just a fraction	$14\% = \frac{14}{100} = \frac{7}{50}$	
	FIACTIONS	out of 100.	100 50	
		Write the percentage over 100 and simplify.		
29.	Increase or	Non-calculator: Find the	Increase 500 by 20% (Non Calc):	
	Decrease by a	percentage and add or	10% of 500 = 50	
	Percentage	subtract it from the original		
		amount.	so 20% of 500 = 100	
			500 + 100 = 600	
		Calculator: Find the percentage multiplier and	Decrease 800 by 17% (Calc):	
		multiply.	100%-17%=83%	
			83% ÷ 100 = 0.83	
			0.83 x 800 = 664	
30.	Percentage Multiplier	The number you multiply a quantity by to increase or	The multiplier for increasing by 12% is 1.12	
		decrease it by a percentage.	The multiplier for decreasing by 12% is 0.88	
			The multiplier for increasing by 100% is 2.	
31.	Reverse	Find the correct percentage	A jumper was priced at £48.60	
	Percentage	given in the question , then work backwards to find 100%.	after a 10% reduction. Find its original price.	
		Look out for words like	100% - 10% = 90%, 90% = £48.60	
		'before' or 'original'.	1% = £0.54 100% = £54	





		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
32.	Simple Interest	Interest calculated as a percentage of the original amount.	£1000 invested for 3 years at 10% simple interest.	
			$10\% \text{ of } \pounds 1000 = \pounds 100$	
33.	Exponential Growth	When we multiply a number repeatedly by the same number (\neq 1), resulting in the number increasing by the same proportion each time.	Interest = $3 \times \pounds 100 = \pounds 300$ 1, 2, 4, 8, 16, 32, 64, 128 is an example of exponential growth, because the numbers are being multiplied by 2 each time.	
		The original amount can grow very quickly in exponential growth.		
34.	Exponential Decay	When we multiply a number repeatedly by the same number $(0 < x < 1)$, resulting in the number decreasing by the same proportion each time.	1000, 200, 40, 8 is an example of exponential decay, because the numbers are being multiplied by $\frac{1}{5}$ each time.	
		The original amount can decrease very quickly in exponential decay.		
35.	Compound Interest	Interest paid on the original amount and the accumulated interest.	A bank pays 5% compound interest a year. Bob invests £3000. How much will he have after 7 years.	
			$3000 \times 1.05^7 = \pounds 4221.30$	
36.	Fraction	A mathematical expression representing the division of one integer by another.	$\frac{2}{7}$ is a 'proper' fraction.	
		Fractions are written as two numbers separated by a horizontal line.	$\frac{9}{4}$ is an 'improper' or 'top-heavy' fraction.	
37.	Numerator	The top number of a fraction.	In the fraction $\frac{3}{5}$, 3 is the numerator.	



	MATHS - YEAR 11 Higher Tier			
	Whole year:			
38.	Denominator	The bottom number of a fraction.	In the fraction $\frac{3}{5}$, 5 is the denominator.	
39.	Unit Fraction	A fraction where the numerator is one and the denominator is a positive integer.	$\frac{1}{2}, \frac{1}{3}, \frac{1}{4}$ etc. are examples of unit fractions.	
40.	Reciprocal	The reciprocal of a number is 1 divided by the number. The reciprocal of x is $\frac{1}{x}$ When we multiply a number by its reciprocal we get 1. This is called the 'multiplicative inverse'.	The reciprocal of 5 is $\frac{1}{5}$ The reciprocal of $\frac{2}{3}$ is $\frac{3}{2}$, because $\frac{2}{3} \times \frac{3}{2} = 1$	
41.	Mixed Number	A number formed of both an integer part and a fraction part .	$3\frac{2}{5}$ is an example of a mixed number.	
42.	Simplifying Fractions	Divide the numerator and denominator by the highest common factor.	$\frac{20}{45} = \frac{4}{9}$	
43.	Equivalent Fractions	Fractions which represent the same value.	$\frac{2}{5} = \frac{4}{10} = \frac{20}{50} = \frac{60}{150} \text{ etc.}$	
44.	Comparing Fractions	To compare fractions, they each need to be rewritten so that they have a common denominator . Ascending means smallest to	Put in to ascending order : $\frac{3}{4}, \frac{2}{3}, \frac{5}{6}, \frac{1}{2}$. Equivalent: $\frac{9}{12}, \frac{8}{12}, \frac{10}{12}, \frac{6}{12}$	
		biggest. Descending means biggest to smallest.	Correct order: $\frac{1}{2}, \frac{2}{3}, \frac{3}{4}, \frac{5}{6}$	
45.	Fraction of an Amount	Divide by the bottom , times by the top .	Find $\frac{2}{5}$ of £60 60 ÷ 5 = 12 12 × 2 = 24	



		MATHS - YEAR 11 Higher Tier		RAG
46.	Whole year: Adding or Subtracting Fractions	Find the LCM of the denominators to find a common denominator. Use equivalent fractions to change each fraction to the common denominator. Then just add or subtract the numerators and keep the denominator the same.	$\frac{2}{3} + \frac{4}{5}$ Multiples of 3: 3, 6, 9, 12, 15 Multiples of 5: 5, 10, 15 LCM of 3 and 5 = 15 $\frac{2}{3} = \frac{10}{15}$ $\frac{4}{5} = \frac{12}{15}$	
			$\frac{10}{15} + \frac{12}{15} = \frac{22}{15} = 1\frac{7}{15}$	
47.	Multiplying Fractions	Multiply the numerators together and multiply the denominators together.	$\frac{3}{8} \times \frac{2}{9} = \frac{6}{72} = \frac{1}{12}$	
48.	Dividing Fractions	 'Keep it, Flip it, Change it - KFC' Keep the first fraction the same. Flip the second fraction upside down. 	$\frac{3}{4} \div \frac{5}{6} = \frac{3}{4} \times \frac{6}{5} = \frac{18}{20} = \frac{9}{10}$	
		Change the divide to a multiply. Multiply by the reciprocal of		
49.	Rounding	the second fraction. To make a number simpler but keep its value close to what it was. If the digit to the right of the rounding digit is less than 5 , round down . If the digit to the right of the	74 rounded to the nearest ten is 70, because 74 is closer to 70 than 80. 152,879 rounded to the nearest thousand is 153,000.	
		rounding digit is 5 or more, round up.		



		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
50.	Decimal Place	The position of a digit to the right of a decimal point .	In the number 0.372, the 7 is in the second decimal place. 0.372 rounded to two decimal places is 0.37, because the 2 tells us to round down. Careful with money - don't write £27.4, instead write £27.40	
51.	Significant Figure	The significant figures of a number are the digits which carry meaning (ie. are significant) to the size of the number. The first significant figure of a number cannot be zero . In a number with a decimal, trailing zeros are not significant.	 In the number 0.00821, the first significant figure is the 8. In the number 2.740, the 0 is not a significant figure. 0.00821 rounded to 2 significant figures is 0.0082. 19357 rounded to 3 significant figures is 19400. We need to include the two zeros at the end to keep the digits in the same place value columns. 	
52.	Truncation	A method of approximating a decimal number by dropping all decimal places past a certain point without rounding .	3.14159265 can be truncated to 3.1415 (note that if it had been rounded, it would become 3.1416).	
53.	Error Interval	A range of values that a number could have taken before being rounded or truncated. An error interval is written using inequalities, with a lower bound and an upper bound. Note that the lower bound inequality can be 'equal to', but the upper bound cannot be 'equal to'.	0.6 has been rounded to 1 decimal place. The error interval is: $0.55 \le x < 0.65$ The lower bound is 0.55 The upper bound is 0.65	



		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
54.	Estimate	To find something close to	An estimate for the height of a	
		the correct answer.	man is 1.8 metres.	
55.	Approximation	When using approximations to	348 + 692 300 + 700	
	••	estimate the solution to a	$\frac{0.526}{0.526} \approx 0.00000000000000000000000000000000000$	
		calculation, round each		
		number in the calculation to		
		1 significant figure.	'Note that dividing by 0.5 is the	
		\approx means 'approximately equal	same as multiplying by 2'	
		to'		
56.	Direct	If two quantities are in direct		
	Proportion	proportion, as one increases ,		
		the other increases by the	$\sqrt{v} = kx$	
		same percentage.	, , , , , , , , , , , , , , , , , , ,	
		If y is directly proportional to		
		x, this can be written as $y \propto$	x	
		x		
			· ↓	
		An equation of the form $y =$		
		<i>kx</i> represents direct proportion, where <i>k</i> is the		
		constant of proportionality.		
57.	Inverse	If two quantities are inversely		
	Proportion	proportional, the product of		
		the two quantities always	^y	
		remains constant, this means	$y = \frac{\kappa}{x}$	
		if one quantity doubles then	*	
		the other quantity will halve .	x	
		If y is inversely proportional		
		to x , this can be written as	Ļ	
		$y \propto \frac{1}{2}$		
		$y \propto \frac{1}{x}$		
		An equation of the form $y = \frac{k}{x}$		
		represents inverse proportion.		
58.	Using	Direct: y = kx or y < x	p is directly proportional to q.	
	proportionality			
	formulae	Inverse: $y = \frac{k}{x}$ or $y \propto \frac{1}{x}$	When p = 12, q = 4.	
		1. Solve to find k using the	Find p when $q = 20$.	
		pair of values in the question.	1. p = kq	
		2. Rewrite the equation using	12 = k x 4	
		the k you have just found.	so k = 3	
		3. Substitute the other given	2. p = 3q	
		value from the question in to		
		the equation to find the missing value.	3. p = 3 x 20 = 60, so p = 60	
		ווויזאווא אמוער.		



	MATHS - YEAR 11 Higher Tier			
	Whole year:			
59.	Direct Proportion with powers	Graphs showing direct proportion can be written in the form $y = kx^n$ Direct proportion graphs will always start at the origin.	Direct Proportion Graphs	
60.	Inverse Proportion with powers	Graphs showing inverse proportion can be written in the form $y = \frac{k}{x^n}$. Inverse proportion graphs will never start at the origin.	Inverse Proportion Graphs $y = \frac{2}{x^2}$ $y = \frac{3}{x^2}$ $y = \frac{35}{x^2}$	
61.	Square Number	The number you get when you multiply a number by itself. Technically these are called 'perfect square numbers' if you go on to study Maths post- 16 you will learn more about this.	1, 4, 9, 16, 25, 36, 49, 64, 81, 100, 121, 144, 169, 196, 225 $9^2 = 9 \times 9 = 81$	
62.	Square Root	The number you multiply by itself to get another number. The reverse process of squaring a number.	$\sqrt{36} = 6$ because $6 \times 6 = 36$	
63.	Solutions to $x^2 = \dots$	Equations involving squares have two solutions , one positive and one negative .	Solve $x^2 = 25$ x = 5 or x = -5 This can also be written as $x = \pm 5$	
64.	Cube Number	The number you get when you multiply a number by itself and itself again.	1, 8, 27, 64, 125 $2^3 = 2 \times 2 \times 2 = 8$	



	MATHS - YEAR 11 Higher Tier				
	Whole year:				
65.	Cube Root	The number you multiply by itself and itself again to get another number.	$\sqrt[3]{125} = 5$ because $5 \times 5 \times 5 = 125$		
		The reverse process of cubing a number.			
66.	Powers of	The powers of a number are that number raised to various powers .	The powers of 3 are: $3^{1} = 3$ $3^{2} = 9$ $3^{3} = 27$ $3^{4} = 81$ etc.		
67.	Multiplication Index Law	When multiplying with the same base (number or letter), add the powers . $a^m \times a^n = a^{m+n}$	$7^5 \times 7^3 = 7^8$ $a^{12} \times a = a^{13}$ $4x^5 \times 2x^8 = 8x^{13}$		
68.	Division Index Law	When dividing with the same base (number or letter), subtract the powers . $a^m \div a^n = a^{m-n}$	$15^{7} \div 15^{4} = 15^{3}$ $x^{9} \div x^{2} = x^{7}$ $20a^{11} \div 5a^{3} = 4a^{8}$		
69.	Brackets Index Laws	When raising a power to another power, multiply the powers together. $(a^m)^n = a^{mn}$	$(y^2)^5 = y^{10}$ $(6^3)^4 = 6^{12}$ $(5x^6)^3 = 125x^{18}$		
70.	Notable Powers	$p = p^1$ $p^0 = 1$ $0^p = 0$, when $p \neq 0$	$99999^0 = 1$		
71.	Negative Powers	A negative power performs the reciprocal. $a^{-m} = \frac{1}{a^m}$	$3^{-2} = \frac{1}{3^2} = \frac{1}{9}$		



	MATHS - YEAR 11 Higher Tier Whole year:				
70	Whole year:		2 2		
72.	Fractional Powers	The denominator of a fractional power acts as a 'root'.	$27^{\frac{2}{3}} = \left(\sqrt[3]{27}\right)^2 = 3^2 = 9$		
		The numerator of a fractional power acts as a normal power. $a^{\frac{m}{n}} = \left(\sqrt[n]{a}\right)^{m}$	$\left(\frac{25}{16}\right)^{\frac{3}{2}} = \left(\frac{\sqrt{25}}{\sqrt{16}}\right)^{3} = \left(\frac{5}{4}\right)^{3} = \frac{125}{64}$		
73.	Surd	The irrational number that is a root of a positive integer , whose value cannot be determined exactly.	$\sqrt{2}$ is a surd because it is a root which cannot be determined exactly.		
		Surds have infinite non- recurring decimals.	$\sqrt{2} = 1.41421356 \dots$ which never repeats.		
74.	Rules of Surds	$\sqrt{ab} = \sqrt{a} \times \sqrt{b}$	$\sqrt{48} = \sqrt{16} \times \sqrt{3} = 4\sqrt{3}$		
		$\sqrt{\frac{a}{b}} = \frac{\sqrt{a}}{\sqrt{b}}$	$\sqrt{\frac{25}{36}} = \frac{\sqrt{25}}{\sqrt{36}} = \frac{5}{6}$		
		$a\sqrt{c}\pm b\sqrt{c}=(a\pm b)\sqrt{c}$	$2\sqrt{5} + 7\sqrt{5} = 9\sqrt{5}$		
		$\sqrt{a} imes \sqrt{a} = a$	$\sqrt{7} \times \sqrt{7} = 7$		



	MATHS - YEAR 11 Higher Tier			RAG
	Whole year:			
75.	Rationalise a Denominator	The process of rewriting a fraction so that the denominator contains only rational numbers .	$\frac{\sqrt{3}}{\sqrt{2}} = \frac{\sqrt{3} \times \sqrt{2}}{\sqrt{2} \times \sqrt{2}} = \frac{\sqrt{6}}{2}$	
			$\frac{6}{3+\sqrt{7}} = \frac{6(3-\sqrt{7})}{(3+\sqrt{7})(3-\sqrt{7})}$ $= \frac{18-6\sqrt{7}}{9-7}$ $= \frac{18-6\sqrt{7}}{2}$ $= 9-3\sqrt{7}$	
76.	Standard Form	$A \times 10^{b}$	8400 = 8.4 x 10 ³	
		where $1 \le A < 10$, b = integer	$0.00036 = 3.6 \times 10^{-4}$	
77.	Multiplying or Dividing with Standard Form	Multiply: Multiply the numbers and add the powers.	$(1.2 \times 10^3) \times (4 \times 10^6) = 8.8 \times 10^9$ $(4.5 \times 10^5) \div (3 \times 10^2)$	
		Divide: Divide the numbers and subtract the powers.	$= 1.5 \times 10^3$	
78.	Adding or Subtracting with Standard Form	Convert in to ordinary numbers, calculate and then convert back in to standard form.	$2.7 \times 10^{4} + 4.6 \times 10^{3}$ $= 27000 + 4600 = 31600$ $= 3.16 \times 10^{4}$	
79.	Expression	A mathematical statement written using symbols, numbers or letters.	$3x + 2$ or $5y^2$	
80.	Equation	A statement showing that two expressions are equal.	2y - 17 = 15	
81.	Identity	An equation that is true for all values of the variables. An identity uses the symbol: ≡	$2x \equiv x + x$	
82.	Formula	Shows the relationship between two or more variables.	Area of a rectangle = length x width or A= LxW	
83.	Expand	To expand a bracket, multiply each term in the bracket by the expression outside the bracket.	3(x+7) = 3x + 21	



	MATHS - YEAR 11 Higher Tier			RAG
	Whole year:			
84.	Factorise	The reverse of expanding. Factorising is writing an expression as a product of terms by 'taking out' a common factor.	6x - 15 = 3(2x - 5), where 3 is the common factor.	
85.	Solve a linear equation	To find the answer/value of something. Use inverse operations on both sides of the equation (balancing method) until you find the value for the letter.	Solve $2x - 3 = 7$ Add 3 on both sides 2x = 10 Divide by 2 on both sides x = 5	
86.	Inverse	Opposite	The inverse of addition is subtraction. The inverse of multiplication is division. The inverse of cubing is cube rooting. The inverse of sine is sine ⁻¹ .	
87.	Substitution	Replace letters with numbers. Be careful of $5x^2$. You need to square first, then multiply by 5.	a = 3, b = 2 and c = 5. Find: 1. $2a = 2 \times 3 = 6$ 2. $3a - 2b = 3 \times 3 - 2 \times 2 = 5$ 3. $7b^2 - 5 = 7 \times 2^2 - 5 = 23$	
88.	Rearranging Formulae	Use inverse operations on both sides of the formula (balancing method) until you find the expression for the letter.	Make x the subject of $y = \frac{2x-1}{z}$ Multiply both sides by z yz = 2x - 1 Add 1 to both sides yz + 1 = 2x Divide by 2 on both sides $\frac{yz + 1}{2} = x$ We now have x as the subject.	



		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
89.	Writing Formulae	Substitute letters for words in the question.	Bob charges £3 per window and a £5 call out charge.	
			C = 3N + 5 Where N=number of windows and	
			C=cost.	
90.	Machine	Takes an input value, performs some operations and produces an output value.		
91.	Function	A relationship between two sets of values.	$f(x) = 3x^2 - 5$ 'For any input value, square the term, then multiply by 3, then subtract 5'.	
92.	Function notation	f(x) x is the input value f(x) is the output value.	f(x) = 3x + 11 Suppose the input value is $x = 5$ The output value is $f(5) = 3 \times 5 + 11 = 26$	
93.	Inverse function	$f^{-1}(x)$ A function that performs the opposite process of the original function. 1. Write the function as $y = f(x)$ 2. Rearrange to make x the subject. 3. Replace the y with x and the x with $f^{-1}(x)$	$f(x) = (1 - 2x)^{5}$. Find the inverse. $y = (1 - 2x)^{5}$ $\sqrt[5]{y} = 1 - 2x$ $1 - \sqrt[5]{y} = 2x$ $\frac{1 - \sqrt[5]{y}}{2} = x$ $f^{-1}(x) = \frac{1 - \sqrt[5]{x}}{2}$	



	MATHS - YEAR 11 Higher Tier				
	Whole year:				
94.	Composite function	A combination of two or more functions to create a new function.	$f(x) = 5x - 3, g(x) = \frac{1}{2}x + 1$ What is $fg(4)$?		
		fg(x) is the composite function that substitutes the function $g(x)$ into the function $f(x)$. fg(x) means 'do g first, then f'	$g(4) = \frac{1}{2} \times 4 + 1 = 3$ $f(3) = 5 \times 3 - 3 = 12 = fg(4)$ What is $fg(x)$? $fg(x) = 5\left(\frac{1}{2}x + 1\right) - 3 = \frac{5}{2}x + 2$		
		gf(x) means 'do f first, then g'			
95.	Iteration	The act of repeating a process over and over again, often with the aim of approximating a desired result more closely. Recursive Notation: $x_{n+1} = \sqrt{3x_n + 6}$	$x_{1} = 4$ $x_{2} = \sqrt{3 \times 4 + 6} = 4.242640 \dots$ $x_{3} = \sqrt{3 \times 4.242640 \dots + 6}$ $= 4.357576 \dots$		
96.	Iterative Method	To create an iterative formula, rearrange an equation with more than one x term to make one of the x terms the subject.	Use an iterative formula to find the positive root of $x^2 - 3x - 6 = 0$ to 3 decimal places. $x_1 = 4$ Answer:		
		You will be given the first value to substitute in, often called x_1 .	$x^{2} = 3x + 6$ $x = \sqrt{3x + 6}$ So $x_{n+1} = \sqrt{3x_{n} + 6}$		
		Keep substituting in your previous answer until your answers are the same to a certain degree of accuracy. This is called converging to a limit.	$x_{1} = 4$ $x_{2} = \sqrt{3 \times 4 + 6} = 4.242640 \dots$ $x_{3} = \sqrt{3 \times 4.242640 \dots + 6}$ $= 4.357576 \dots$ Keep repeating		
		Use the 'ANS' button on your calculator to keep substituting in the previous answer.	$x_7 = 4.372068 = 4.372 (3dp)$ $x_8 = 4.372208 = 4.372 (3dp)$ So answer is $x = 4.372 (3dp)$		



		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
97.	Simplifying	Collect 'like terms'.	2x + 3y + 4x - 5y + 3	
	Expressions	Be careful with negatives.	= 6x - 2y + 3	
		x^2 and x are not like terms.	$3x + 4 - x^{2} + 2x - 1$ = 5x - x ² + 3	
98.	x times x	The answer is x^2 not $2x$.	Squaring is multiplying by itself, not by 2.	
99.	$p \times p \times p$	The answer is p^3 not $3p$.	If p = 2, then p^3 = 2x2x2=8, not 2x3 = 6	
100	p + p + p	The answer is 3p not p^3 .	If p = 2, then $2+2+2 = 6$, not $2^3 = 8$	
101	Quadratic	A quadratic expression is of the form	Examples of quadratic expressions:	
			<i>x</i> ²	
		$ax^2 + bx + c$	$8x^2 - 3x + 7$	
		where a, b and c are numbers,	Examples of non-quadratic expressions:	
		$a \neq 0$.	$2x^3 - 5x^2$	
			9x - 1	
102	Factorising Quadratics	When a quadratic expression is in the form $x^2 + bx + c$ find the two numbers that add to give b and multiply to give c.	$x^{2} + 7x + 10 = (x + 5)(x + 2)$ (because 5 and 2 add to give 7 and multiply to give 10) $x^{2} + 2x - 8 = (x + 4)(x - 2)$ (because +4 and -2 add to give	
103	Difference of 2 Squares	An expression of the form $a^2 - b^2$ can be factorised to give $(a + b)(a - b)$.	+2 and multiply to give -8) $x^{2} - 25 = (x + 5)(x - 5)$ $16x^{2} - 81 = (4x + 9)(4x - 9)$	
104	Expanding double brackets	When you expand double brackets use the FOIL method to make sure you don't forget any of the terms!	First Outer Inner Last $x^2+6\chi+3\chi+18$ $=x^2+9\chi+18$	



		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
105	Solving Quadratics $(ax^2 = b)$	Isolate the x^2 term and square root both sides. Remember there will be a	$2x^2 = 98$ $x^2 = 49$	
		positive and a negative solution.	$x = \pm 7$	
106	Solving Quadratics $(ax^2 + bx = 0)$	Factorise and then solve = 0.	$x^{2} - 3x = 0$ $x(x - 3) = 0$ $x = 0 \text{ or } x = 3$	
107	Solving Quadratics by Factorising	Factorise the quadratic in the usual way.	x = 0 or x = 3 Solve $x^2 + 3x - 10 = 0$	
	Factorising $(a = 1)$	Solve = 0	Factorise: $(x + 5)(x - 2) = 0$ x = -5 or x = 2	
		Make sure the equation = 0 before factorising.		
108	Factorising Quadratics	When a quadratic is in the form	Factorise $6x^2 + 5x - 4$	
	when $a \neq 1$	$ax^2 + bx + c$ 1. Multiply a by c = ac	1. $6 \times -4 = -24$	
		2. Find two numbers that add to give b and multiply to give ac.	 2. Two numbers that add to give +5 and multiply to give -24 are +8 and -3 	
		3. Re-write the quadratic, replacing bx with the two numbers you found.	3. $6x^2 + 8x - 3x - 4$	
		4. Factorise in pairs - you should get the same bracket twice	4. Factorise in pairs:	
		5. Write your two brackets - one will be the repeated bracket, the other will be made of the factors outside each of the two brackets.	2x(3x + 4) - 1(3x + 4) 5. Answer = $(3x + 4)(2x - 1)$	



	MATHS - YEAR 11 Higher Tier			RAG
	Whole year:			
109	Solving Quadratics by	Factorise the quadratic in the usual way.	Solve $2x^2 + 7x - 4 = 0$	
	Factorising $(a \neq 1)$	Solve = 0 Make sure the equation = 0	Factorise: $(2x - 1)(x + 4) = 0$	
110	Quadratic	before factorising. A 'U-shaped' curve called a	$x = \frac{1}{2} \text{ or } x = -4$	
	Graph	parabola.		
		The equation is of the form $y = ax^2 + bx + c$, where a , b and c are numbers, $a \neq 0$.	-1 (2, -9)	
		If $a < 0$, the parabola is upside down.		
111	Roots of a Quadratic	A root is a solution.		
		The roots of a quadratic are the <i>x</i> -intercepts of the quadratic graph.		
112	Turning Point of a Quadratic	A turning point is the point where a quadratic turns.		
		On a positive parabola, the turning point is called a minimum.		
		On a negative parabola, the turning point is called a maximum.		
113.	Completing the Square (when $a = 1$)	A quadratic in the form $x^2 + bx + c$ can be written in the form $(x + p)^2 + q$	Complete the square of $y = x^2 - 6x + 2$	
		1. Write a set of brackets with <i>x</i> in and half the value of <i>b</i> .	Answer: $(x-3)^2 - 3^2 + 2$	
		2. Square the bracket.	$=(x-3)^2-7$	
		3. Subtract $\left(\frac{b}{2}\right)^2$ and add <i>c</i> .	The minimum value of this expression occurs when $(x - x)$	
		4. Simplify the expression.	$(x^2)^2 = 0$, which occurs when $x = 3$	
		This helps you find the maximum or minimum of a	When $x = 3$, $y = 0 - 7 = -7$	
		quadratic graph.	Minimum point = $(3, -7)$	



		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
114	Completing the Square (when	A quadratic in the form $ax^2 + by$	Complete the square of	
	$a \neq 1$)	bx + c can be written in the form $p(x + q)^2 + r$.	$4x^2 + 8x - 3$	
		Use the same method as	Answer:	
		above, but factorise out a at the start.	$4[x^2+2x]-3$	
			$= 4[(x+1)^2 - 1^2] - 3$	
			$=4(x+1)^2-4-3$	
			$=4(x+1)^2-7$	
115	Solving Quadratics by	Complete the square in the usual way and use inverse	Solve $x^2 + 8x + 1 = 0$	
	Completing the	operations to solve.	Answer:	
	Square		$(x+4)^2 - 4^2 + 1 = 0$	
			$(x+4)^2 - 15 = 0$	
			$(x+4)^2 = 15$	
			$(x+4) = \pm \sqrt{15}$	
			$x = -4 \pm \sqrt{15}$	
116	Solving	A quadratic in the form ax^2 +	Solve $3x^2 + x - 5 = 0$	
	Quadratics using the	bx + c = 0 can be solved using the formula:	Answer:	
	Quadratic		a = 3, b = 1, c = -5	
	Formula	$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$	$-1 \pm \sqrt{1^2 - 4 \times 3 \times -5}$	
		Use the formula if the	$x = \frac{-1 \pm \sqrt{1^2 - 4 \times 3 \times -5}}{2 \times 3}$	
		quadratic does not factorise easily.	$x = \frac{-1 \pm \sqrt{61}}{6}$	
			6 x = 1.14 or -1.47 (2 d. p.)	
			x = 1.1707 1.77 (2 u. p.)	
117	Coordinates	Written in pairs. The first term is the x-coordinate (movement across). The second term is the y- coordinate (movement up or down).	A: $(4,7)$ B: $(-6,-3)$ B: $(-6,-3)$	



		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
118	Midpoint of a Line	Method 1: add the x coordinates and divide by 2, add the y coordinates and divide by 2.	Find the midpoint between (2,1) and (6,9) $\frac{2+6}{2} = 4 \text{ and } \frac{1+9}{2} = 5$	
		Method 2: Sketch the line and find the values half way between the two x and two y values.	So, the midpoint is (4,5)	
119	Linear Graph	Straight line graph. The general equation of a linear graph is y = mx + c where m is the gradient and c is the y-intercept. The equation of a linear graph can contain an x-term, a y- term and a number.	Example: $\begin{array}{c} & & & & \\ & & & & \\ & & & & \\ & & & &$	
120	Plotting Linear Graphs	Method 1: Table of Values Construct a table of values to calculate coordinates. Method 2: Gradient-Intercept Method (use when the equation is in the form $y = mx + c$) 1. Plots the y-intercept 2. Using the gradient, plot a second point. 3. Draw a line through the two points plotted.	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	3 6



		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
	Plotting Linear Graphs	Method 3: Cover-Up Method (use when the equation is in the form $ax + by = c$)	9↑ 8 7 6	
		1. Cover the x term and solve the resulting equation. Plot this on the $x - axis$.		
		2. Cover the y term and solve the resulting equation. Plot this on the $y - axis$.	$3 - 2 - 1 - 1 - 1 - 1 - 2 - 3 - 4 - 6 - 7 - 8 \rightarrow 1 - 1 - 2 - 3 1$	
		3. Draw a line through the two points plotted.		
121	Gradient	The gradient of a line is how steep it is.	Gradient = $4/2 = 2$	
		Gradient =	Gradient = -3/1 =-3	
		$\frac{Change \text{ in } y}{Change \text{ in } x} = \frac{Rise}{Run}$		
		The gradient can be positive (sloping upwards) or negative (sloping downwards)		
122	Finding the Equation of a Line given a point and a gradient	Substitute in the gradient (m) and point (x,y) in to the equation $y = mx + c$ and solve for c.	Find the equation of the line with gradient 4 passing through (2,7).	
			y = mx + c	
			$7 = 4 \times 2 + c$	
			c = -1	
			y = 4x - 1	





		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
123	Finding the Equation of a	Use the two points to calculate the gradient. Then	Find the equation of the line passing through (6,11) and (2,3)	
	Line given two points	repeat the method above using the gradient and either of the points.	$m = \frac{11 - 3}{6 - 2} = 2$	
			y = mx + c	
			$11 = 2 \times 6 + c$	
			c = -1 $y = 2x - 1$	
			y = 2x = 1	
124	Parallel Lines	If two lines are parallel, they will have the same gradient. The value of m will be the same for both lines.	Are the lines $y = 3x - 1$ and 2y - 6x + 10 = 0 parallel?	
			Answer:	
			Rearrange the second equation in to the form $y = mx + c$	
			$2y - 6x + 10 = 0 \rightarrow y = 3x - 5$	
			Since the two gradients are equal (3), the lines are parallel.	
125	Perpendicular Lines	If two lines are perpendicular, the product of their gradients will always equal -1.	Find the equation of the line perpendicular to $y = 3x + 2$ which passes through (6,5)	
		The gradient of one line will	Answer:	
		be the negative reciprocal of the gradient of the other line.	As they are perpendicular, the gradient of the new line will be	
		You may need to rearrange	$-\frac{1}{3}$ as this is the negative reciprocal of 3.	
		equations of lines to compare gradients (they need to be in	y = mx + c	
		the form $y = mx + c$)	$5 = -\frac{1}{3} \times 6 + c$	
			c = 7	
			$y = -\frac{1}{3}x + 7$	
			Or	
			3x + x - 7 = 0	



	MATHS - YEAR 11 Higher Tier			RAG
	Whole year:			
126	Linear Sequence	A number pattern with a common difference.	2, 5, 8, 11 is a linear sequence	
127	Term	Each value in a sequence is called a term.	In the sequence 2, 5, 8, 11, 8 is the third term of the sequence.	
128	Term-to-term rule	A rule which allows you to find the next term in a sequence if you know the previous term.	First term is 2. Term-to-term rule is 'add 3' Sequence is: 2, 5, 8, 11	
129	nth term	A rule which allows you to calculate the term that is in the nth position of the sequence. Also known as the 'position- to-term' rule. n refers to the position of a term in a sequence.	nth term is $3n - 1$ The 100th term is $3 \times 100 - 1 = 299$	
130	Finding the nth term of a linear sequence	 Find the difference. Multiply that by <i>n</i>. Substitute n = 1 to find out what number you need to add or subtract to get the first number in the sequence. 	Find the nth term of: 3, 7, 11, 15 1. Difference is +4 2. Start with $4n$ 3. $4 \times 1 = 4$, so we need to subtract 1 to get 3. nth term = $4n - 1$	
131	Fibonacci type sequences	A sequence where the next number is found by adding up the previous two terms	The Fibonacci sequence is: 1,1,2,3,5,8,13,21,34 An example of a Fibonacci-type sequence is: 4, 7, 11, 18, 29	



		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
132	Geometric	A sequence of numbers where	An example of a geometric	
	Sequence	each term is found by	sequence is:	
		multiplying the previous one	sequence is.	
		by a number called the	2, 10, 50, 250	
		common ratio, r.	The common ratio is 5	
			Another example of a geometric	
			sequence is:	
			81, -27, 9, -3, 1	
			The common ratio is $-\frac{1}{3}$	
			3	
133	Quadratic	A sequence of numbers where		
	Sequence	the second difference is		
	-	constant.	2 6 12 20 30 42	
		constant.	+4 +6 +8 +10 +12	
			+2 +2 +2 +2	
		A quadratic sequence will		
		have a n^2 term.		
134	Triangular	The sequence which comes	1 3 6 10	
	numbers	from a pattern of dots that		
		form a triangle.		
		Torm a changle.		
		1, 3, 6, 10, 15, 21		
		1,0,0,10,10,21		
135	Inequality	An inequality says that two	7 ≠ 3	
	mequaticy	values are not equal.	/ / J	
			$x \neq 0$	
		$a \neq b$ means that a is not		
		equal to b.		
136	Inequality	x > 2 means x is greater than	State the integers that satisfy	
	symbols	2		
		x < 3 means x is less than 3	$-2 < x \le 4.$	
		u > 1 moone v is greater than		
		$x \ge 1$ means x is greater than	-1, 0, 1, 2, 3, 4	
		or equal to 1		
		$x \le 6$ means x is less than or		
		equal to 6		



		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
137	Inequalities on a Number Line	Inequalities can be shown on a number line.	-2 -1 0 1 2 3	
		Open circles are used for numbers that are less than or greater than (< or >)	$x \ge 0$	
		Closed circles are used for numbers that are less than or equal or greater than or equal $(\leq or \geq)$	-5 -4 -3 -2 -1 0 1 2 3 4 5 x < 2	
			-5 -4 -3 -2 -1 0 1 2 3 4 5 $-5 \le x < 4$	
138	Graphical	Inequalities can be	Shade the region that satisfies:	
	Inequalities	represented on a coordinate grid.	$y > 2x, x > 1 and y \le 3$	
		If the inequality is strict $(x > 2)$ then use a dotted line.	y = 2x	
		If the inequality is not strict $(x \le 6)$ then use a solid line.	y = 3	
		Shade the region which satisfies all the inequalities.	x = 1	





		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
139	Quadratic Inequalities	Sketch the quadratic graph of the inequality.	Solve the inequality $x^2 - x - 12 < 0$	
		If the expression is $> or \ge$ then the answer will be above the x-axis. If the expression is $< or \le$ then the answer will be below	Sketch the quadratic:	
		the x-axis. Look carefully at the inequality symbol in the question.	The required region is below the x-axis, so the final answer is:	
		Look carefully if the quadratic is a positive or negative parabola.	-3 < x < 4 If the question had been > 0, the answer would have been:	
			x < -3 or x > 4	
140	Set Notation	A set is a collection of things, usually numbers, denoted with brackets { }	{3, 6, 9} is a set. $\begin{cases} x \mid x > 0 \\ \uparrow & \uparrow & \downarrow \end{cases}$	
		$\{x \mid x \ge 7\}$ means 'the set of all x's, such that x is greater than or equal to 7'	the set of all x such that x is greater than zero	
		The 'x' can be replaced by any letter.	$\{x: -2 \le x < 5\}$	
		Some people use ':' instead of 'I'		
141	Simultaneous Equations	A set of two or more equations, each involving two or more variables (letters).	2x + y = 7 $3x - y = 8$	
		The solutions to simultaneous equations satisfy both/all of the equations.	x = 3 $y = 1$	
142	Variable	A symbol, usually a letter, which represents a number which is usually unknown.	In the equation $x + 2 = 5$, x is the variable.	



	MATHS - YEAR 11 Higher Tier				
	Whole year:				
143	Coefficient	A number used to multiply a variable.	6z		
			6 is the coefficient		
		It is the number that comes before/in front of a letter.	z is the variable		
144	Solving Simultaneous Equations (by Elimination)	 Balance the coefficients of one of the variables. Eliminate this variable by adding or subtracting the equations (Same Sign Subtract, Different Sign Add) Solve the linear equation you get using the other variable. Substitute the value you found back into one of the previous equations. Solve the equation you get. Check that the two values you get satisfy both of the original equations. 	5x + 2y = 9 10x + 3y = 16 Multiply the first equation by 2. 10x + 4y = 18 10x + 3y = 16 Same Sign Subtract (+10x on both) y = 2 Substitute $y = 2$ in to equation. $5x + 2 \times 2 = 9$ 5x + 4 = 9 5x = 5 x = 1		
145	Solving Simultaneous Equations (by Substitution)	 Rearrange one of the equations into the form y = or x = Substitute the right-hand side of the rearranged equation into the other equation. Expand and solve this equation. Substitute the value into the y = or x = equation. Check that the two values you get satisfy both of the original equations. 	Solution: $x = 1, y = 2$ y - 2x = 3 3x + 4y = 1 Rearrange: $y - 2x = 3 \rightarrow y =$ 2x + 3 Substitute: $3x + 4(2x + 3) = 1$ Solve: $3x + 8x + 12 = 1$ 11x = -11 x = -1 Substitute: $y = 2 \times -1 + 3$ y = 1 Solution: $x = -1, y = 1$		



		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
146	Solving Simultaneous Equations	Draw the graphs of the two equations.	y = 2x - 1	
	(Graphically)	The solutions will be where the lines meet.		
		The solution can be written as a coordinate.	y = 5 - x and $y = 2x - 1$. They meet at the point with coordinates (2,3) so the answer is $x = 2$ and $y = 3$	
147	Linear Graph	Straight line graph.	Example:	
		The equation of a linear graph can contain an x-term, a y- term and a number.	5 ⁴ Y	
		Examples:		
		x = y	-5 4 ·3 ·2 1 ·1 · 2 ·3 4 5	
		y = 4		
		x = -2	38	
		y = 2x - 7	5	
		y + x = 10		
		2y - 4x = 12		
148	Quadratic Graph	A 'U-shaped' curve called a parabola.	y y = x ² -4x-5	
		The equation is of the form	-1 5 x	
		$y = ax^2 + bx + c$, where a, b and c are numbers, $a \neq 0$.	(2, -9)	
		If $a < 0$, the parabola is upside down.		





		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
149	Cubic Graph	The equation is of the form $y = ax^3 + k$, where k is an number.		
		If $a > 0$, the curve is increasing.		
		If $a < 0$, the curve is decreasing.		
150	Reciprocal Graph	The equation is of the form $y = \frac{A}{x}$, where A is a number and $x \neq 0$.	$y \uparrow$	
		The graph has asymptotes on the x-axis and y-axis.		
151	Asymptote	A straight line that a graph approaches but never touches.	y horizontal asymptote	
			vertical asymptot	
152	Exponential Graph	The equation is of the form $y = a^x$, where a is a number called the base. If $a > 1$ the graph increases.		
		If $0 < a < 1$, the graph decreases.	2 0 2 2	
		The graph has an asymptote which is the x-axis.		





	MATHS - YEAR 11 Higher Tier			RAG
	Whole year:			
153	$y = \sin x$	Key Coordinates:		
		(0,0), (90,1), (180,0), (270, -1), (
		<i>y</i> is never more than 1 or less than -1.	90° 180° 270° 360° 450° 540° 630° 720° - 1.0	
		Pattern repeats every 360°.		
154	$y = \cos x$	Key Coordinates:		
		(0,1), (90,0), (180, -1),	graph of y = cosine θ	
		(270,0), (360,1)	90 180° 270° 360° 450° 540° 630° 720°	
		<i>y</i> is never more than 1 or less than -1.	90° 180° 270° 360° 450° 540° 630° 720° - 1.0	
		Pattern repeats every 360°.		
155	$y = \tan x$	Key Coordinates:		
		(0,0), (45,1), (135, -1), (180,0),	y graph of y= tan θ	
		(225,1), (315, -1), (360,0)		
		Asymptotes at $x = 90$ and $x = 270$ Pattern repeats every 360°.	θ 90° 180° 270° 360° 450° 540° 630° 720° -2 -4	
156	f(x) + a	Vertical translation up a units. $\binom{0}{a}$	f(x) y f(x) + 3	
			$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	





		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
157		Horizontal translation left a units. $\begin{pmatrix} -a \\ 0 \end{pmatrix}$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	
158	-f(x)	Reflection over the x-axis.	-f(x) x $f(x)$ $f($	
159	<i>f</i> (- <i>x</i>)	Reflection over the y-axis.	f(-x) = y = f(x) $f(x) = y = f(x)$ $f(x) = y = y = y$ $f(x) = y = y$ $f(x) = y = y$ $f(x) = y$	
160	Area Under a Curve	To find the area under a curve, split it up into simpler shapes - such as rectangles, triangles and trapeziums - that approximate the area.	(y_{u}) $(y_{$	
161	Tangent to a Curve	A straight line that touches a curve at exactly one point.	Y Tangent line	



		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
162		The gradient of a curve at a point is the same as the gradient of the tangent at that point.		
		1. Draw a tangent carefully at the point.		
		2. Make a right-angled triangle.	Time (hours)	
		3. Use the measurements on the axes to calculate the rise and run (change in y and change in x)	$Gradient = \frac{Change in y}{Change in x}$ $= \frac{16}{2} = 8$	
		4. Calculate the gradient.	$=\frac{1}{2}=8$	
163	Rate of Change	The rate of change at a particular instant in time is represented by the gradient of the tangent to the curve at that point.	Negative rate of change o 2 4 6 8 There (s)	
164	Distance-Time Graphs	You can find the speed from the gradient of the line (Distance ÷ Time)	Distance (Km)	
		The steeper the line, the quicker the speed.		
		A horizontal line means the object is not moving (stationary).	Time (Hours)	
165	Velocity-Time Graphs	You can find the acceleration from the gradient of the line (Change in Velocity ÷ Time)	Velocity 2	
		The steeper the line, the quicker the acceleration.	(m/s)	
		A horizontal line represents no acceleration, meaning a constant velocity.	Time (Seconds)	
		The area under the graph is the distance.		





	MATHS - YEAR 11 Higher Tier				
	Whole year:				
166	Equation of a Circle	The equation of a circle, centre (0,0), radius r, is:	$y_{1} = \frac{y_{1}}{5} (x, y) = x^{2} + y^{2} = 25$		
		$x^2 + y^2 = r^2$			
167	Tangent	A straight line that touches a	A		
		circle at exactly one point, never entering the circle's interior.	c GG.s		
		A radius is perpendicular to a tangent at the point of contact.			
168	Gradient	Gradient is another word for slope. $G = \frac{Rise}{Run} = \frac{Change in y}{Change in x}$ $= \frac{y_2 - y_1}{x_2 - x_1}$	(x_{2},y_{2}) $B (-3, 4)$ $GRADIENT between$ $A at (3,-2) and B at (-3)$ $m = \frac{y_{2} - y_{1}}{x_{2} - x_{1}}$ $m = \frac{4 - 2}{-3 - 3}$ $m = 6/-6 = 1 \sqrt{2}$		
169	Polygon	A 2D shape with only straight edges.	Rectangle, Hexagon, Decagon, Kite etc.		
170	Regular	A shape is regular if all the sides and all the angles are equal.	Some examples:		
171	Names of	3-sided = Triangle			
	Polygons	4-sided = Quadrilateral	Triangle Quadrilateral Pentagon Hexagon		
		5-sided = Pentagon			
		6-sided = Hexagon	Heptagon Octagon Nonagon Decagon		
		7-sided = Heptagon			
		8-sided = Octagon			
		9-sided = Nonagon			
		10-sided = Decagon			



		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
172		A prism is a 3D shape whose cross section is the same throughout.	Triangle Prism Pentagonal Prism Hexagonal Prism	
	Cross Section	The cross section is the shape that continues all the way through the prism.	Cross Section	
174	Net	A pattern that you can cut and fold to make a model of a 3D shape.	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	
	Properties of Solids	Faces = flat surfaces Edges = sides/lengths Vertices = corners	A cube has 6 faces, 12 edges and 8 vertices.	
176	Plans and Elevations	This takes 3D drawings and produces 2D drawings. Plan View: from above Side Elevation: from the side Front Elevation: from the front	2D Drawings Plan Front Elevation Side Elevation	



	MATHS - YEAR 11 Higher Tier			
	Whole year:			
177		A method for visually representing 3D objects in 2D.	2cm 4cm 4cm	
178	Types of Angles	Acute angles are less than 90°. Right angles are exactly 90°.	Acute Right Obtuse Reflex	
		Obtuse angles are greater than 90° but less than 180°. Reflex angles are greater than 180° but less than 360°.		
179	Angle Notation	Can use one lower-case letters, eg. θ or x Can use three upper-case letters, eg. <i>BAC</i>		
180	Angles at a Point	Angles around a point add up to 360°.	$\frac{d}{c} a$ $a+b+c+d = 360^{\circ}$	
181	Angles on a Straight Line	Angles around a point on a straight line add up to 180°.	$x y$ $x + y = 180^{\circ}$	
182	Opposite Angles	Vertically opposite angles are equal.	$\frac{x}{y}$	
183	Alternate Angles	Alternate angles are equal. They look like Z angles, but never say this in the exam.	x y	



	MATHS - YEAR 11 Higher Tier			
	Whole year:			
184		Corresponding angles are equal.		
		They look like F angles, but never say this in the exam.	x	
185	Co-Interior Angles	Co-Interior angles add up to 180°.	$y x \rightarrow$	
		They look like C angles, but never say this in the exam.	<u>x y</u>	
186	Angles in a Triangle	Angles in a triangle add up to 180°.	B 45° 55° C	
187	Types of Triangles	Right Angle Triangles have a 90° angle in. Isosceles Triangles have 2 equal sides and 2 equal base angles.	Right Angled Isosceles	
		Equilateral Triangles have 3 equal sides and 3 equal angles (60°).	60'	
		Scalene Triangles have different sides and different angles.	60° 60° Equilateral Scalene	
		Base angles in an isosceles triangle are equal.		
188	Angles in a Quadrilateral	Angles in a quadrilateral add up to 360°.	65 ⁰ 93 0	
189	Sum of Interior Angles	$(n-2) \times 180$ where n is the number of sides.	Sum of Interior Angles in a Decagon = $(10 - 2) \times 180 =$ 1440°	



		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
190		$\frac{(n-2) \times 180}{n}$ You can also use the formula: 180 - Size of Exterior Angle	Size of Interior Angle in a Regular Pentagon = $\frac{(5-2) \times 180}{5} = 108^{\circ}$	
191	Size of Exterior Angle in a Regular Polygon	$\frac{360}{n}$ You can also use the formula: $180 - Size \ of \ Interior \ Angle$	Size of Exterior Angle in a Regular Octagon = $\frac{360}{8} = 45^{\circ}$	
192	Perimeter	The total distance around the outside of a shape. Units include: <i>mm</i> , <i>cm</i> , <i>m</i> etc.	8 cm 5 cm P = 8 + 5 + 8 + 5 = 26cm	
193	Area	The amount of space inside a shape. Units include: mm^2, cm^2, m^2		
194	Area of a Rectangle	Length x Width	4 cm $A = 36 cm^2$	
195	Area of a Parallelogram	Base x Perpendicular Height Not the slanted height.	4 cm $3 cm7 cmA = 21 \text{cm}^2$	



		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
196	Area of a Triangle	Base x Height ÷ 2	9 4 5 12 $A = 24cm^2$	
197	Area of a Trapezium	$\frac{(a+b)}{2} \times h$ "Half the sum of the parallel side, times the height between them. That is how you calculate the area of a trapezium"	6 cm 5 cm 16 cm $(a = 6, b = 16, h = 5)$ $A = 55 \text{ cm}^2$	
198	Compound Shape	A shape made up of a combination of other shapes put together		
199	Surface Area	The total area of the surface of a three- dimensional object.	The surface area of a cube is the area of all 6 faces added together.	
200	Volume	Volume is a measure of the amount of space inside a solid shape. Units: mm^3 , cm^3 , m^3 etc.		



	MATHS - YEAR 11 Higher Tier				
	Whole year:				
201	Volume of a Cube/Cuboid	V = Area of Cross Section × Length	6cm		
		Volume = area of cross-section x length	3 cm		
		Volume = 5 x 3 x length			
		Volume = $15 \times 6 = 90 \text{ cm}^2$			
202	Volume of a Prism	$V = Area of Cross Section$ $\times Length$ $V = A \times L$	Area of cross section		
		$V - A \wedge L$	Length		
203	Circle	A circle is the locus of all points equidistant from a central point.	(· ŕ		
204	Parts of a Circle	 Radius - the distance from the centre of a circle to the edge Diameter - the total distance across the width of a circle through the centre. Circumference - the total distance around the outside of a circle Chord - a straight line whose end points lie on a circle Tangent - a straight line which touches a circle at exactly one point Arc - a part of the circumference of a circle Sector - the region of a circle enclosed by two radii and their intercepted arc Segment - the region bounded by a chord and the arc created by the chord 	Parts of a Circle Radius Diameter Circumference Chord Arc Tangent Segment Sector		





		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
205	Area of a Circle	$A = \pi r^2$ which means 'pi x	If the radius was 5cm, then:	
		radius squared'.		
			$A = \pi \times 5^2 = 78.5 cm^2$	
206	Circumference	$C = \pi d$ which means 'pi x	If the radius was 5cm, then:	
	of a Circle	diameter'	$C = \pi \times 10 = 31.4cm$	
207	π ('pi')	Pi is the circumference of a	Γ S-VAR ₁ P Γ DISTR ₁ n Γ ►r∠θ ₁ Poł	
		circle divided by the	2 3 +	
		diameter.	Ran# π DRG▶	
			• EXP Ans	
		$\pi \approx 3.14$		
208	Arc Length of a	The arc length is part of the	Arc Length = $\frac{115}{360} \times \pi \times 8 =$	
	Sector	circumference.		
			8.03 <i>cm</i>	
		Take the angle given as a	Acm B	
		fraction over 360° and	0	
		multiply by the	1150	
		circumference.		
			A	
209	Area of a	The area of a sector is part of	Area = $\frac{115}{360} \times \pi \times 4^2 = 16.1 cm^2$	
	Sector	the total area.	360	
			o 4cm B	
		Take the angle given as a	0	
		fraction over 360° and	115 ⁰	
		multiply by the area.		
			A	
210	Volume of a	$V = \pi r^2 h$		
	Cylinder			
			1	
			E and	
			5cm	
			2cm	
			v	
			$V = \pi(4)(5)$	
			$= 62.8 cm^3$	



		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
211	Surface Area of a Cylinder	Curved Surface Area = πdh or $2\pi rh$ Total SA = $2\pi r^2 + \pi dh$ or $2\pi r^2 + 2\pi rh$	$5cm$ $Total SA = 2\pi(2)^{2} + \pi(4)(5) = 28\pi$	
212	Volume of a Cone	$V = \frac{1}{3}\pi r^2 h$ This formula will be given to you in the exam.	$V = \frac{1}{3}\pi(4)(5)$ $= 20.9cm^{3}$	
	Surface Area of a Cone	This formula will be given to you in the exam: Curved Surface Area = πrl where $l = slant$ height This formula will <u>NOT</u> be given to you in the exam: Total SA = $\pi rl + \pi r^2$ You may need to use Pythagoras' Theorem to find the slant height	$5m \sqrt{3m}$ $Total SA = \pi(3)(5) + \pi(3)^2$ $= 24\pi$	
214	Surface Area of a Sphere	This formula will be given to ye $SA = 4\pi r^2$ Look out for hemispheres - halve the SA of a sphere and add on a circle (πr^2)	Find the surface area of a sphere with radius 3cm. $SA = 4\pi(3)^2 = 36\pi cm^2$	



	MATHS - YEAR 11 Higher Tier			
	Whole year:			
215		$Volume = \frac{1}{3}Bh$ where B = area of the base This formula will <u>NOT</u> be given to you in the exam This formula will be given to you in the exam:	$V = \frac{1}{3} \times 6 \times 6 \times 7 = 84cm^{3}$ Find the volume of a sphere with diameter 10cm.	
		$V = \frac{4}{3}\pi r^{3}$ Look out for hemispheres - just halve the volume of a sphere.	$V = \frac{4}{3}\pi(5)^3 = \frac{500\pi}{3}cm^3$	
217	Frustums	A frustum is a solid (usually a cone or pyramid) with the top removed. Find the volume of the whole shape, then take away the volume of the small cone/pyramid removed at the top.	$V = \frac{1}{3}\pi(10)^{2}(24) - \frac{1}{3}\pi(5)^{2}(12)$ = 700\pi cm^{3}	
218	Metric System for Length	A system of measures based on: - the metre for length Length: mm, cm, m, km	1kilometres = 1000 metres 1 metre = 100 centimetres 1 centimetre = 10 millimetres	
219	Metric System for Mass	A system of measures based on: - the kilogram for mass Mass: mg, g, kg, tonne	1 tonne = 1000 kilograms 1 kilogram = 1000 grams 1 gram = 1000 milligrams	



		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
220	Metric System for Volume	A system of measures based on:	1 litre = 1000 millilitres	
		the litre for volume	$1 \ centilitre = 10 \ millilitres$	
		- the litre for volume Volume: ml, cl, l	1 litre = 100 centilitre	
221	•	A system of weights and	1lb = 16 ounces	
	System	measures originally developed in England, usually based on	1 foot = 12 inches	
		human quantities	$1 \ gallon = 8 \ pints$	
		Length: inch, foot, yard, miles		
		Mass: lb, ounce, stone		
		Volume: pint, gallon		
222	Metric and	Use the unitary method to	5 miles ≈ 8 kilometres	
	Imperial Units	nperial Units convert between metric and imperial units.	$1 \ gallon \approx 4.5 \ litres$	
			2.2 pounds \approx 1 kilogram	
			1 inch = 2.5 centimetres	
223	Scale	The ratio of the length in a model to the length of the real thing.	Scale 1:10	
			Real HorseDrawn Horse1500 mm high150 mm high2000 mm long200 mm long	
224	Scale (Map)	The ratio of a distance on the map to the actual distance in real life.	1 in. = 250 mi 1 cm = 160 km	





		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
225		1. Measure from North (draw a North line)	The bearing of \underline{B} from \underline{A}	
		2. Measure clockwise	A	
		3. Your answer must have 3 digits (eg. 047°)		
		Look out for where the bearing is measured from.	The bearing of \underline{A} from \underline{B}	
226	Compass Directions	You can use an acronym such as 'Never Eat Shredded Wheat' to remember the order of the compass directions in a clockwise direction.		
		Bearings: $NE = 045^\circ$, $W = 270^\circ etc$.		
227	1	Angles in a semi-circle have a right angle at the circumference.	$y = 90^{\circ}$ $x = 180 - 90 - 38 = 52^{\circ}$	
228	Circle Theorem 2	Opposite angles in a cyclic quadrilateral add up to 180° .		



		MATHS - YEAR 11		RAG
	Whole years	Higher Tier		
229	Whole year: Circle Theorem 3	The angle at the centre is twice the angle at the circumference. \sqrt{a}	$x = 104 \div 2 = 52^{\circ}$	
230	Circle Theorem 4	Angles in the same segment are equal.	$x = 42^{\circ}$ $y = 31^{\circ}$	
231	Circle Theorem 5	A tangent is perpendicular to the radius at the point of contact.	y = 5cm (Pythagoras' Theorem)	





		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
232	Circle Theorem 6	Tangents from an external point at equal in length.	$\frac{4 \text{cm}}{3 \text{cm}}$	
233	Circle Theorem 7	Alternate Segment Theorem	$x = 52^{\circ}, y = 38^{\circ}$	
234	Speed, Distance, Time	Speed = Distance ÷ Time Distance = Speed x Time Time = Distance ÷ Speed D S T Remember the correct units.	Speed = 4mph Time = 2 hours Find the Distance. $D = S \times T = 4 \times 2 = 8$ miles	
235	Density, Mass, Volume	Density = Mass ÷ Volume Mass = Density x Volume Volume = Mass ÷ Density	Density = 8kg/m^3 Mass = 2000g Find the Volume. $V = M \div D = 2 \div 8 = 0.25m^3$ Remember the correct units.	



		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
236	Pressure,	Pressure = Force ÷ Area	Pressure = 10 Pascals	
	Force, Area	Force = Pressure x Area	Area = 6cm²	
		Area = Force ÷ Pressure	Find the Force	
		F p X A Remember the correct units.	$F = P \times A = 10 \times 6 = 60 N$	
237	Distance-Time Graphs	You can find the speed from the gradient of the line (Distance ÷ Time)	Distance (Km)	
		The steeper the line, the quicker the speed.	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	
		A horizontal line means the object is not moving (stationary).		
238	Congruent Shapes	Shapes are congruent if they are identical - same shape and same size.		
		Shapes can be rotated or reflected but still be congruent.		
239	Congruent Triangles	4 ways of proving that two triangles are congruent:	$A \underbrace{\begin{array}{c} C \\ G1' \\ 73' \\ 73' \\ Bcm \end{array}}^{C} Bcm F$	
		1. SSS (Side, Side, Side)	ь V Е	
		2. RHS (Right angle, Hypotenuse, Side)	$BC = DF$ $\angle ABC = \angle EDF$	
		3. SAS (Side, Angle, Side)	$\angle ABC = \angle EDF$ $\angle ACB = \angle EFD$	
		4. ASA (Angle, Side, Angle) or AAS	∴ The two triangles are congruent by AAS.	
		ASS does not prove congruency.		





		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
240	Similar Shapes	Shapes are similar if they are the same shape but different sizes.		
		The proportion of the matching sides must be the same, meaning the ratios of corresponding sides are all equal.		
241	Scale Factor	The ratio of corresponding sides of two similar shapes.	16 10 15	
		To find a scale factor, divide a length on one shape by the corresponding length on a similar shape.	Scale Factor = $15 \div 10 = 1.5$	
242	Finding missing	1. Find the scale factor.	2cm 3cm	
	lengths in similar shapes	2. Multiply or divide the corresponding side to find a missing length.	4.5cm	
		If you are finding a missing length on the larger shape you will need to multiply by the scale factor.		
		If you are finding a missing length on the smaller shape you will need to divide by the scale factor.	Scale Factor = $3 \div 2 = 1.5$ $x = 4.5 \times 1.5 = 6.75cm$	
243	Similar Triangles	To show that two triangles are similar, show that:		
		1. The three sides are in the same proportion		
		2. Two sides are in the same proportion, and their included angle is the same		
		3. The three angles are equal		



MATHS - YEAR 11							
	Higher Tier						
	Whole year:						
244	Parallel	Parallel lines never meet.					
245	Perpendicular	Perpendicular lines are at right angles. There is a 90° angle between them.					
246	Vertex	A corner or a point where two lines meet.	vertex A C C				
247	Angle Bisector	 Angle Bisector: Cuts the angle in half. 1. Place the sharp end of a pair of compasses on the vertex. 2. Draw an arc, marking a point on each line. 3. Without changing the compass put the compass on each point and mark a centre point where two arcs cross over. 4. Use a ruler to draw a line through the vertex and centre point. 	Angle Bisector				





		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
248	Perpendicular Bisector	Perpendicular Bisector: Cuts a line in half and at right angles.	\mathbf{X}	
		1. Put the sharp point of a pair of compasses on A.	Line Bisector	
		2. Open the compass over half way on the line.		
		3. Draw an arc above and below the line.		
		4. Without changing the compass, repeat from point B.		
		5. Draw a straight line through the two intersecting arcs.		
249	Perpendicular from an External Point	The perpendicular distance from a point to a line is the shortest distance to that line.	P	
		1. Put the sharp point of a pair of compasses on the point.	X	
		2. Draw an arc that crosses the line twice.		
		3. Place the sharp point of the compass on one of these points, open over half way and draw an arc above and below the line.		
		4. Repeat from the other point on the line.		
		5. Draw a straight line through the two intersecting arcs.		





		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
250	Perpendicular from a Point on a Line	Given line PQ and point R on the line:		
		1. Put the sharp point of a pair of compasses on point R.	P S R T Q	
		 Draw two arcs either side of the point of equal width (giving points S and T) 		
		3. Place the compass on point S, open over halfway and draw an arc above the line.		
		4. Repeat from the other arc on the line (point T).		
		5. Draw a straight line from the intersecting arcs to the original point on the line.		
251	Triangles (Side,	1. Draw the base of the triangle using a ruler.		
	Side, Side)	2. Open a pair of compasses to the width of one side of the triangle.		
		3. Place the point on one end of the line and draw an arc.		
		4. Repeat for the other side of the triangle at the other end of the line.		
		5. Using a ruler, draw lines connecting the ends of the base of the triangle to the point where the arcs intersect.		





	MATHS - YEAR 11 Higher Tier					
	Whole year:					
252		1. Draw the base of the triangle using a ruler.	Â			
	Angle, Side)	2. Measure the angle required using a protractor and mark this angle.	B 50° 7cm			
		3. Remove the protractor and draw a line of the exact length required in line with the angle mark drawn.				
		4. Connect the end of this line to the other end of the base of the triangle.				
253	Constructing Triangles	1. Draw the base of the triangle using a ruler.	×			
	(Angle, Side, Angle)	2. Measure one of the angles required using a protractor and mark this angle.	y <u>42°</u> <u>51°</u> Z 8.3cm			
		3. Draw a straight line through this point from the same point on the base of the triangle.				
		4. Repeat this for the other angle on the other end of the base of the triangle.				
254	Constructing an Equilateral	1. Draw the base of the triangle using a ruler.	C			
	Triangle (also makes a 60° angle)	2. Open the pair of compasses to the exact length of the side of the triangle.				
		3. Place the sharp point on one end of the line and draw an arc.	A B			
		4. Repeat this from the other end of the line.				
		5. Using a ruler, draw lines connecting the ends of the base of the triangle to the point where the arcs intersect.				





	MATHS - YEAR 11 Higher Tier						
	Whole year:						
255	Loci and Regions	A locus is a path of points that follow a rule. For the locus of points closer	AB				
		to B than A, create a perpendicular bisector between A and B and shade the side closer to B.	Points Closer to B than A.				
		For the locus of points equidistant from A, use a compass to draw a circle, centre A.	, 2cm A A A				
			Points less than Points more than 2cm from A 2cm from A				
		For the locus of points equidistant to line X and line Y, create an angle bisector.	r D E				
		For the locus of points a set distance from a line, create two semi-circles at either end joined by two parallel lines.					
256	Equidistant	A point is equidistant from a set of objects if the distances between that point and each of the objects is the same.					



	MATHS - YEAR 11 Higher Tier						
	Whole year:						
257	Pythagoras' Theorem	For any right angled triangle: $a^2 + b^2 = c^2$	y Finding a Shorter Side 10 SUBTRACT: 8				
		a c b	a = y, b = 8, c = 10 $a^{2} = c^{2} - b^{2}$ $y^{2} = 100 - 64$ $y^{2} = 36$ y = 6				
		Used to find missing lengths.					
		a and b are the shorter sides, c is the hypotenuse (longest side).					
258	3D Pythagoras' Theorem	Find missing lengths by identifying right angled triangles.	Can a pencil that is 20cm long fit in a pencil tin with dimensions 12cm, 13cm and 9cm? The pencil tin is in the shape of a cuboid.				
		You will often have to find a missing length you are not asked for before finding the missing length you are asked	Hypotenuse of the base = $\sqrt{12^2 + 13^2} = 17.7$				
		for.	Diagonal of cuboid = $\sqrt{17.7^2 + 9^2} = 19.8cm$				
			No, the pencil cannot fit.				
	Trigonometry	The study of triangles.					
260	Hypotenuse	The longest side of a right- angled triangle.	hypotenuse				
		Is always opposite the right angle.					
261	Adjacent	Next to	P atisodido R Adjacent Q				





MATHS - YEAR 11 Higher Tier					
	Whole year:				
262.	Trigonometric Formulae	Use SOHCAHTOA. $\sin \theta = \frac{O}{H}$	x 35°		
		$\sin \theta = \frac{H}{H}$ $\cos \theta = \frac{A}{H}$	Use 'Opposite' and 'Adjacent',		
		$\tan \theta = \frac{O}{A}$	so use 'tan' $\tan 35 = \frac{x}{11}$		
			$x = 11 \tan 35 = 7.70 cm$		
		S H C H T A When finding a missing angle,	7cm x		
		use the 'inverse' trigonometric function by pressing the 'shift' button on the calculator.	5cm Use 'Adjacent' and 'Hypotenuse', so use 'cos' $\cos x = \frac{5}{7}$		
			$x = \cos^{-1}\left(\frac{5}{7}\right) = 44.4^{\circ}$		
263	3D Trigonometry	Find missing lengths by identifying right angled triangles.	A B		
		You will often have to find a missing length you are not asked for before finding the missing length you are asked for.			





	MATHS - YEAR 11 Higher Tier					RAG			
	Whole year:								
264	5								
	values		0°	30°	45°	0.00	0.00	7	
				30*	45	60°	90°	-	
		$\sin \theta$	$\frac{\sqrt{0}}{2}$	$\frac{\sqrt{1}}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{4}}{2}$		
						-		-	
		$\cos \theta$	$\frac{\sqrt{4}}{2}$	$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{1}}{2}$	$\frac{\sqrt{0}}{2}$		
			2		2	2	2	-	
		$\tan \theta$	0	$\frac{\sqrt{3}}{3}$	1	√ 3	±∞		
				152				1	
265	Translation	Transl		eans t	o mov	'e a		R	
		shape					Q		
		The sh	nape d	loes no	ot cha	nge	3	3 ▼ 4 ► R'	
		size oi	r orier	ntatior	า.		•		
								4 » P'	
266	Column Vector	In a co	olumn	vecto	r, the	top	(2	$\frac{2}{1}$ mapping (2 right 2 up)	
		numbe				-	: (3	$\binom{2}{3}$ means '2 right, 3 up'	
		(+) an							
		moves	moves up (+) or down (-)			•)	(-	-1)	
							(_	$\binom{-1}{-5}$ means '1 left, 5 down'	
267	Rotation	The size	ze doe	es not	chang	e, but	R	otate Shape A 90° anti-	
		the sh			-			ockwise about (0,1)	
		point.							
			•					Y	
		Use tr	acing	paper	•				
							-		
							-		
							17		
							X		
							•	Υ.	



MATHS - YEAR 11 Higher Tier					
	Whole year:	~			
268		The size does not change, but the shape is 'flipped' like in a mirror.	Reflect shape C in the line $y = x$		
		Line $x = ?$ is a vertical line.	5 B		
		Line $y = ?$ is a horizontal line.			
		Line $y = x$ is a diagonal line.	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		
269	Enlargement	The shape will get bigger or smaller. Multiply each side by the scale factor.	Scale Factor = 3 means '3 times larger = multiply by 3'		
			Scale Factor = ½ means 'half the size = divide by 2'		
270	Finding the Centre of Enlargement	Draw straight lines through corresponding corners of the two shapes. The centre of enlargement is the point where all the lines cross over. Be careful with negative enlargements as the corresponding corners will be the other way around.	A to B is an enlargement SF 2 about the point (2,1)		
271	Describing Transformations	Give the following information when describing each transformation: Look at the number of marks in the question for a hint of how many pieces of information are needed. If you are asked to describe a 'transformation', you need to say the name of the type of transformation as well as the other details.	 Translation, Vector Rotation, Direction, Angle, Centre Reflection, Equation of mirror line Enlargement, Scale factor, Centre of enlargement 		



		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
272	Fractional Scale Factor Enlargements	A fractional enlargement makes a shape smaller.	10 ⁴ 9 8 7 6 5 4 3 2 1 1 2 2 1 1 2 3 4 5 6 7 7 6 6 7 7 6 6 7 7 7 6 7 7 7 6 7	
273	Negative Scale Factor Enlargements	Negative enlargements will look like they have been rotated. SF = -2 will be rotated, and also twice as big.	Enlarge ABC by scale factor -2, centre (1,1)	
274	Invariance	A point, line or shape is invariant if it does not change/move when a transformation is performed. An invariant point 'does not vary'.	If shape P is reflected in the $y - axis$, then exactly one vertex is invariant.	
275	Hypothesis	A hypothesis is a statement that might be true or false but you haven't got enough evidence to support it either way YET. A hypothesis must be testable.	For example: Children who go to bed earlier score higher on their class tests	



		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
276		The data Cycle has five parts to it: 1. Planning		
		 2. Collecting Data 3. Processing and Representing data 4. Interpreting results Communicating results clearly and evaluating methods 		
277	Constraints	During the planning phase you should consider the constraints of your investigation: • Time • Cost • Convenience • Ethical issues Confidentiality	For example, people might not want to answer personal questions about their age or where they live.	
278	Primary	Data which you have collected yourself	For example, you do a survey on your classmates about their favourite food	
279	Secondary	Data which someone else has collected	For example, you use census data to investigate national trends in salaries	
280	Quantitative	Numerical data	For example, how many siblings you have or how tall you are	
281	Qualitative	Descriptive data (using words not numbers)	For example, your favourite food	
	Discrete	Numerical (quantitative) data which can be counted	For example, how many siblings you have	
283	Continuous	Numerical (quantitative) data which can be measured	For example, your mass or height	



	MATHS - YEAR 11 Higher Tier					
	Whole year:					
284		Data that has been bundled in to categories.	Foot length, <i>l</i> , (cm) Number of children $10 \le l < 12$ 5 $12 \le l < 17$ 53			
		Seen in grouped frequency tables, histograms, cumulative frequency etc.				
285	Population	The whole group you are interested in	e.g. the population of the UK			
286	Sample	A group selected from the population	e.g. the students in our school			
287	Biased sample	A sample that does not properly represent the population				
288	Random Sample	A sample where each member of the population has an equal chance of being selected for the sample				
289	Mean	Add up the values and divide by how many values there are.	The mean of 3, 4, 7, 6, 0, 4, 6 is $\frac{3+4+7+6+0+4+6}{7} = 5$			
290	Mean from a Table	 Find the midpoints (if necessary) Multiply Frequency by values or midpoints Add up these values Divide this total by the Total Frequency If grouped data is used, the answer will be an estimate. 	Height in cm Frequency Midpoint $F \times M$ $0 < h \le 10$ 8 5 $8 \times 5 = 40$ $10 < h \le 30$ 10 20 $10 \times 20 = 200$ $30 < h \le 40$ 6 35 $6 \times 35 = 210$ Total 24 Ignore! 450 Estimated Mean height: $450 \div 24 =$ 18.75 cm			



		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
291	Median Value	The middle value.	Find the median of: 4, 5, 2, 3, 6, 7, 6	
		Put the data in order and find the middle one.	Ordered: 2, 3, 4, 5, 6, 6, 7	
		If there are two middle values, find the number half way between them by adding them together and dividing by 2.	Median = 5	
292	Median from a Table	Use the formula $\frac{(n+1)}{2}$ to find the position of the median.	If the total frequency is 15, the median will be the $\left(\frac{15+1}{2}\right) =$ 8 <i>th</i> position	
		n is the total frequency.		
293	Mode /Modal	Most frequent/common.	Find the mode: 4, 5, 2, 3, 6, 4,	
	Value	Can have more than one mode (called bi-modal or multi- modal) or no mode (if all values appear once)	7, 8, 4 Mode = 4	
294	Range	Highest value subtract the Smallest value	Find the range: 3, 31, 26, 102, 37, 97.	
		Range is a 'measure of spread'. The smaller the range the more consistent the data.	Range = 102-3 = 99	
295	Outlier	A value that 'lies outside' most of the other values in a set of data.	12 10 Outlier 8 6	
		An outlier is much smaller or much larger than the other values in a set of data.		
296	Lower Quartile	Divides the bottom half of the data into two halves.	Find the lower quartile of: 2, 3, 4, 5, 6, 6, 7	
		$LQ = Q_1 = \frac{(n+1)}{4}th \text{ value}$	$Q_1 = \frac{(7+1)}{4} = 2nd \text{ value } \rightarrow 3$	

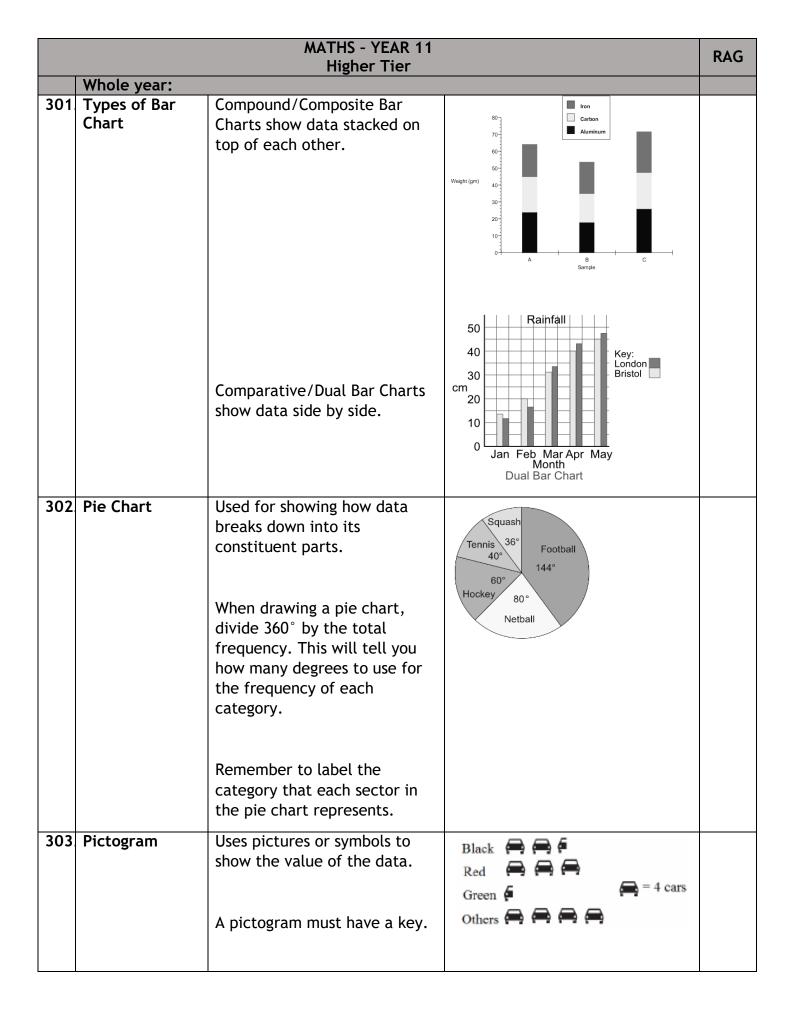




MATHS - YEAR 11 Higher Tier					
	Whole year:				
297	Lower Quartile	Divides the top half of the data into two halves.	Find the upper quartile of: 2, 3, 4, 5, 6, 6, 7		
		$UQ = Q_3 = \frac{3(n+1)}{4}th \text{ value}$	$Q_3 = \frac{3(7+1)}{4} = 6th \text{ value } \rightarrow 6$		
298	Interquartile Range	The difference between the upper quartile and lower quartile.	Find the IQR of: 2, 3, 4, 5, 6, 6, 7		
		$IQR = Q_3 - Q_1$	$IQR = Q_3 - Q_1 = 6 - 3 = 3$		
		The smaller the interquartile range, the more consistent the data.			
299	Frequency Table	A record of how often each value in a set of data occurs.	Number of marksTally marksFrequency1##1 72##153##1 64##155 3Total26		
300	Bar Chart	Represents data as vertical blocks. x - axis shows the type of data y - axis shows the frequency for each type of data Each bar should be the same width There should be gaps between	Number of pets owned		
		each bar Remember to label each axis.			









		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
304	Line Graph	h A graph that uses points connected by straight lines to show how data changes in values.		
		This can be used for time series data, which is a series of data points spaced over uniform time intervals in time order.	0 1 2 3 4 5 6 7 8 9	
305	Two Way Tables	A table that organises data around two categories.	Question: Complete the 2 way table below. Left Handed Right Handed Total Boys 10 58 58 Girls 0 100 100	
		Fill out the information step by step using the information given.	Total 84 100 Answer: Step 1, fill out the easy parts (the totals) Total Left Handed Right Handed Total Boys 10 48 58 Girls 42 42 Total 16 84 100	
		Make sure all the totals add up for all columns and rows.	Answer: Step 2, fill out the remaining partsLeft HandedRight HandedTotalBoys104858Girls63642Total1684100	
306	Box Plots	The minimum, lower quartile, median, upper quartile and maximum are shown on a box plot.		
		A box plot can be drawn independently or from a cumulative frequency diagram.	Minimum L.Q Median U.Q Maximum	
307	Comparing Box	Write two sentences.	'On average, students in class A	
	Plots	1. Compare the averages using the medians for two sets of data.	were more successful on the test than class B because their median score was higher.'	
		2. Compare the spread of the data using the range or IQR for two sets of data.	'Students in class B were more consistent than class A in their	
		The smaller the range/IQR, the more consistent the data.	test scores as their IQR was smaller.'	
		You must compare box plots in the context of the problem.		



		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
308		A frequency polygon is plotted against the mid-points of the data groups and is drawn with a ruler.	FREQUENCY POLYGON	
309	Cumulative frequency	A cumulative frequency diagram is plotted against the end-points of the data groups and is drawn free-hand with a smooth curve shape. They can be used to find the median (half-way) and quartile (25% and 75%) values	14 19 12 10 8 4 4 6 6 6 6 6 6 7 7 7 7 7 7 7 7 7 7 7 7	
310	Histogram	Histograms are used for representing continuous data with unequal class widths. Bars must not have gaps between them	LO LO LO LO LO LO LO LO LO LO LO LO LO L	
311	Frequency density	The frequency density can be found using this formula: frequency density = <u>frequency</u> class width	Freq F.D. Width	
312	Correlation	Correlation between two sets of data means they are connected in some way.	There is correlation between temperature and the number of ice creams sold.	
313	Causality	When one variable influences another variable.	The more hours you work at a particular job (paid hourly), the higher your income from that job will be.	



		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
314	Scatter Graph	A graph in which values of two variables are plotted along two axes to compare them and see if there is any connection between them.	Scatterplet ler quelity characteristic XXX.	
315	Positive Correlation	As one value increases the other value increases.	$ \begin{array}{c} $	
316	Negative Correlation	As one value increases the other value decreases.		
317	No Correlation	There is no linear relationship between the two.	y + + + + + + + + + + + + + + + + + + + x	
318	Strong Correlation	When two sets of data are closely linked. The correlation may be positive or negative.	A stronger negative correlation is shown here.	
319	Weak Correlation	When two sets of data have correlation, but are not closely linked. The correlation may be positive or negative.	A weaker positive correlation is shown here.	



		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
320	Line of Best Fit (or regression line)	A straight line that best represents the data on a scatter graph.	x x x x x x x x x x x x x x x	
321	Outlier	A value that 'lies outside' most of the other values in a set of data. An outlier is much smaller or much larger than the other values in a set of data.	12 10 8 6 4 2 0 20 40 60 80 100	
322	Probability	The likelihood/chance of something happening. Is expressed as a number between 0 (impossible) and 1 (certain). Can be expressed as a fraction, decimal, percentage or in words (likely, unlikely, even chance etc.)	Impossible Unlikely Even Chance Likely Certain 1-in-6 Chance 4-in-5 Chance	
323	Probability Notation	P(A) refers to the probability that event A will occur.	P(Red Queen) refers to the probability of picking a Red Queen from a pack of cards.	
	Theoretical Probability	Number of Favourable Outcomes Total Number of Possible Outcomes	Probability of rolling a 4 on a fair 6-sided die = $\frac{1}{6}$.	
	Relative Frequency	Number of Successful Trials Total Number of Trials	A coin is flipped 50 times and lands on Tails 29 times. The relative frequency of getting Tails = $\frac{29}{50}$.	
326	Expected Outcomes	To find the number of expected outcomes, multiply the probability by the number of trials.	The probability that a football team wins is 0.2 How many games would you expect them to win out of 40? $0.2 \times 40 = 8 \text{ games}$	



		MATHS - YEAR 11 Higher Tier									RAG
	Whole year:										
327		Outcomes are exhaustive if they cover the entire range of possible outcomes. The probabilities of an exhaustive set of outcomes	Whe outc exha all tl	ome lustiv	s 1, ve, t	2, 3 beca	, 4, ! use †	5 an they	d 6 a cov	are	
328	Mutually	adds up to 1. Events are mutually exclusive	Exan	nple	s of	muti	uallv	v exc	lusi	/e	
	Exclusive	if they cannot happen at the same time. The probabilities of an exhaustive set of mutually exclusive events adds up to 1.	ever - Tui - Hei Exan excli	nts: rning ads a nple:	g left and ⁻ s of 1	t and Tails non	d rig on a mut	ht a co [.]	in		
			- Kin card King	g an s, be	d He ecau	earts se yo	s froi				
329	Frequency Tree	A diagram showing how information is categorised into various categories. The numbers at the ends of branches tells us how often something happened (frequency).	\subset	BOYS Giris		L8 Doe	Wears g Wears g	ar glasses	\sim		
		The lines connected the numbers are called branches.									
330	Sample Space	The set of all possible outcomes of an experiment.	+ 1 2 3 4	1 2 3 4 5	2 3 4 5 6	3 4 5 6 7	4 5 6 7 8	5 6 7 8 9	6 7 8 9 10		
			5 6	6 7	7 8	8 9	9 10	10 11	11 12		





	MATHS - YEAR 11 Higher Tier					
	Whole year:					
331	Combination	A collection of things, where the order does not matter.	How many combinations of two ingredients can you make with apple, banana and cherry?			
			Apple, Banana			
			Apple, Cherry			
			Banana, Cherry			
			3 combinations			
332	Permutation	A collection of things, where the order does matter.	You want to visit the homes of three friends, Alex (A), Betty (B) and Chandra (C) but haven't decided the order. What choices do you have?			
			ABC			
			ACB			
			BAC			
			BCA			
			САВ			
			СВА			
333.	Permutations with Repetition	When something has n different types, there are n choices each time.	How many permutations are there for a three-number combination lock?			
		Choosing r of something that has n different types, the permutations are:	10 numbers to choose from $\{1, 2, \dots, 10\}$ and we choose 3 of them \rightarrow			
		$n \times n \times (r \ times) = n^r$	$10 \times 10 \times 10 = 10^3 = 1000$ permutations.			
334	Permutations without Repetition	We have to reduce the number of available choices each time.	How many ways can you order 4 numbered balls?			
		One you have chosen something, you cannot choose it again.	$4 \times 3 \times 2 \times 1 = 24$			



		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:	5		
335		If there are x ways of doing something and y ways of doing something else, then there are xy ways of performing both.	To choose one of $\{A, B, C\}$ and one of $\{X, Y\}$ means to choose one of $\{AX, AY, BX, BY, CX, CY\}$ The rule says that there are 3 ×	
336	Tree Diagrams	Tree diagrams show all the possible outcomes of an event and calculate their probabilities.	$2 = 6 \text{ choices.}$ $Bag A Bag B$ $\frac{1}{3} \text{ red}$ $\frac{1}{5} \text{ red}$	
		All branches must add up to 1 when adding downwards. This is because the probability of something not happening is 1 minus the probability that it does happen. Multiply going across a tree diagram. Add going down a tree diagram.	4 5 6 1 3 1 3 1 3 1 3 1 3 1 3 1 3 1 3 1 3 1 3 1 3 1 3 1 1 3 1 1 3 1 1 1 1 1 1 1 1 1 1	
337.	Independent Events	The outcome of a previous event does not influence/affect the outcome of a second event.	An example of independent events could be replacing a counter in a bag after picking it.	
338	Dependent Events	The outcome of a previous event does influence/affect the outcome of a second event.	An example of dependent events could be not replacing a counter in a bag after picking it. 'Without replacement'	





MATHS - YEAR 11 Higher Tier							
	Whole year:						
339	Probability Notation	P(A) refers to the probability that event A will occur.	P(Red Queen) refers to the probability of picking a Red Queen from a pack of cards.				
		P(A') refers to the probability that event A will not occur.	P(Blue') refers to the probability that you do not pick Blue.				
		$P(A \cup B)$ refers to the probability that event A or B or both will occur.	P(Blonde ∪ Right Handed) refers to the probability that you pick someone who is Blonde or Right Handed or both.				
		$P(A \cap B)$ refers to the probability that both events A and B will occur.	P(Blonde ∩ Right Handed) refers to the probability that you pick someone who is both Blonde and Right Handed.				
340	Venn Diagrams	A Venn Diagram shows the relationship between a group of different things and how they overlap. You may be asked to shade Venn Diagrams as shown below and to the right.	$A \cup B$ $A \cap B$ $A \cup B'$				





		MATHS - YEAR 11 Higher Tier		RAG
	Whole year:			
341	Venn Diagram Notation	∈ means 'element of a set' (a value in the set)	Set A is the even numbers less than 10.	
		<pre>{ } means the collection of values in the set.</pre>	$A = \{2, 4, 6, 8\}$	
		ξ means the 'universal set' (all the values to consider in the question)	Set B is the prime numbers less than 10. B = {2, 3, 5, 7}	
		A' means 'not in set A' (called complement)	A ∪ B = {2, 3, 4, 5, 6, 7, 8}	
		A ∪ B means 'A or B or both' (called Union)	A ∩ B = {2}	
		$A \cap B$ means 'A and B (called Intersection)		
342	AND rule for Probability	When two events, A and B, are independent:	What is the probability of rolling a 4 and flipping a Tails?	
		$P(A \text{ and } B) = P(A) \times P(B)$	$P(4 and Tails) = P(4) \times P(Tails)$	
			$=\frac{1}{6} \times \frac{1}{2} = \frac{1}{12}$	
343	OR rule for Probability	When two events, A and B, are mutually exclusive:	What is the probability of rolling a 2 or rolling a 5?	
		P(A or B) = P(A) + P(B)	P(2 or 5) = P(2) + P(5)	
			$=\frac{1}{6}+\frac{1}{6}=\frac{2}{6}=\frac{1}{3}$	
344	Conditional Probability	The probability of an event A happening, given that event B has already happened.	1st Bead 2nd Bead	
		With conditional probability, check if the numbers on the second branches of a tree diagram changes. For example, if you have 4 red beads in a bag of 9 beads and pick a red bead on the first pick, then there will be 3 red beads left out of 8 beads on	$\begin{array}{c c} \frac{4}{9} & \text{Red} & \frac{5}{8} & \text{Green} \\ \hline \frac{5}{9} & \text{Green} & \frac{4}{8} & \text{Red} \\ \hline \frac{4}{8} & \text{Green} & \frac{4}{8} & \text{Green} \\ \end{array}$	
		the second pick.		



